

**MULTIPLIERLESS TWO-CHANNEL PERFECT RECONSTRUCTION LATTICE FILTER BANK DESIGN USING SPECTRAL FACTOR SELECTION**

Mingazin A.

RADIS Ltd, Russia, Moscow, Zelenograd, 124460, POB 20.  
Tel./fax (095) 535-35-13, e-mail: [alexmin@orc.ru](mailto:alexmin@orc.ru)

A two-channel perfect reconstruction lattice filter bank proposed in [1] is considered. We have assumed that involvement of a spectral factor selection into multiplierless lattice filter bank design algorithms can improve results. It is confirmed by the design example at nominal edges  $f_{1n}=0.18$ ,  $f_{2n}=0.32$  and the sampling frequency equal 1. We used two algorithms based on a variation of initial parameters (VIP) as [4]. The results [2-4] may be improved by using a special spectral factor. That is shown in Table1. Here 2N-1 is the order of each filter in the bank; C is the spectral factor code; M is the fractional part wordlength of coefficients; m is the number of non-zero bits in coefficients;  $f_1$  and r are the passband edge and auxiliary parameter [4] for which the solution is obtained;  $\tilde{a}_0$  - the minimum stop-band attenuation;  $\Sigma$ - the total number of adders including the structure adders (first item) and adders (second item) replacing all pairs of multipliers on coefficients  $\alpha_i$  in Fig.1b in [2,3].

Table 1

Algorithm	2N-1	C	M	m	$f_1; r$	$\tilde{a}_0, \text{ dB}$	$\Sigma$
Simple rounding [2]	27	0	10	2	-	25.38	56=28+14×2
Tree search [2]					-	45.37*	56=28+14×2
Implicit enumeration [3]	21		9	≤ 3	-	45.19*	56=22+17×2
VIP [4]					0.18053; 3	45.01	56=22+17×2
VIP	27	0	10	≤ 2	0.1950; 0.1683	38.85	52=28+12×2
		33	8		0.1788; 0.1367	46.79	54=28+13×2
			7		0.1794; 0.1429	44.06	50=28+11×2
VIP + variation of coefficients (coordinate-wise search)	27	0	10	0.1780; 0.4398	40.98	50=28+11×2	
		33	10	0.1788; 0.1367	48.10	56=28+14×2	
				0.1800; 0.1481	47.81	54=28+13×2	
			7	0.1786; 0.1377	46.08	50=28+11×2	
				0.1810; 0.1600	44.38	44=28+8×2	

In case C=0 the passband zeros of the transfer function are  $R_6 \exp(\pm j\phi_6)$ ,  $R_5 \exp(\pm j\phi_5), \dots, R_1 \exp(\pm j\phi_1)$ ,  $R_0$  and in case C=33 the zeros are  $R_6 \exp(\pm j\phi_6)$ ,  $R_5^{-1} \exp(\pm j\phi_5), R_4 \exp(\pm j\phi_4), \dots, R_1 \exp(\pm j\phi_1)$ ,  $R_0^{-1}$ . Here  $R_i$  is the radius and  $\phi_i$  is the angle of i-th zero in z-plane. In addition  $R_i < 1$ ,  $i=0,1,\dots,6$  and  $\phi_1 < \phi_2 < \dots < \phi_6$ . For the solution with  $\tilde{a}_0=48.10$  dB the coefficients are  $\alpha_0, \dots, \alpha_{13}$ :  $-2 + 2^{-3}$ ,  $2^{-1} + 2^{-7}$ ,  $2^{-1} + 2^{-5}$ ,  $2^{-5} - 2^{-8}$ ,  $2^{-1} + 2^{-6}$ ,  $2^3 - 1$ ,  $-2^{-1} - 2^{-7}$ ,  $2^{-2} - 2^{-6}$ ,  $1 - 2^{-7}$ ,  $-2^{-6} + 2^{-8}$ ,  $-2^{-3} + 2^{-5}$ ,  $2^{-3} + 2^{-6}$ ,  $-2^{-4} + 2^{-6}$ ,  $2^{-6} - 2^{-10}$ . For the solution with  $\tilde{a}_0=46.08$  dB all coefficients are identical except  $\alpha_3, \alpha_9, \alpha_{13}$ :  $2^{-5}, -2^{-6}, 2^{-6}$ . It is interesting that the solution with  $\tilde{a}_0=46.79$  dB differs from the one with  $\tilde{a}_0=48.10$  dB by the only coefficient  $\alpha_{13} = 2^{-6}$ . The values  $\tilde{a}_0$  marked with the badge \* are reevaluated at 1000 points for the coefficients from [2,3].

**References**

- Vaidyanathan P.P., Hoang P.Q. Lattice structures for optimal and robust implementation of two-channel perfect-reconstruction QMF banks. IEEE Trans. on ASSP. 1988. V. 36. Jan. P. 81-94.
- Lim Y.C., Yu Y. J. A width-recursive depth-first tree search approach for the design of discrete coefficient perfect reconstruction lattice filter bank. IEEE Trans. on CAS: II. 2003. Vol. 50. June. P. 257-266.
- Yli-Kaakinen J., Saramaki T., Bregovic R. An algorithm for the design of multiplierless two-channel perfect reconstruction orthogonal lattice filter banks. ISCCSP. 2004. Mar. P. 415-418.
- Mingazin A. Design of multiplierless perfect reconstruction lattice filter banks. Sowremennaya elektronika. 2007. Mar. P. 50-55.